# Nonlinear Analysis

## Theory, Methods & Applications

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# NONLINEAR ANALYSIS
## THEORY, METHODS & APPLICATIONS



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# Volume Contents

## Volume 20 Number 1


| | | |
|---|---|---|
| R. PRECUP | 1 | On the topological transversality principle |
| R. LUI | 11 | Stability of travelling wave solutions for a bistable evolutionary ecology model |
| F. ALI MEHMETI and S. NICAISE | 27 | Nonlinear interaction problems |
| M. F. BETTA and A. MERCALDO | 63 | Comparison and regularity results for a nonlinear elliptic equation |
| SOFTWARE SURVEY SECTION | I | |


## Volume 20 Number 2


| | | |
|---|---|---|
| D. O'REGAN | 79 | Existence of solutions to some differential delay equations |
| G. DÍAZ and R. LETELIER | 97 | Explosive solutions of quasilinear elliptic equations: existence and uniqueness |
| O. SCHERZER, H. W. ENGL and R. S. ANDERSSEN | 127 | Parameter identification from boundary measurements in a parabolic equation arising from geophysics |
| S. CARL, S. HEIKKILÄ and M. KUMPULAINEN | 157 | On a generalized iteration method with applications to fixed point theorems and elliptic systems involving discontinuities |
| D. BUGAJEWSKI and S. SZUFLA | 169 | Kneser's theorem for weak solutions of the Darboux problem in Banach spaces |
| M. M. TOM | 175 | Existence of global solutions for nonlinear dispersive equations |
| CORRIGENDUM | 191 | |
| SOFTWARE SURVEY SECTION | I | |

## Volume 20 Number 3


| | | |
|---|---|---|
| S. S. Cheng and W. T. Patula | 193 | An existence theorem for a nonlinear difference equation |
| N. Kikuchi | 205 | Kneser's property for a parabolic partial differential equation |
| S. K. Ntouyas, Y. G. Sficas and P. Ch. Tsamatos | 215 | An existence principle for boundary value problems for second order functional differential equations |
| O. Goubet | 223 | Nonlinear Galerkin methods using hierarchical almost-orthogonal finite elements bases |
| W. Zhao | 249 | Normal structure coefficients and seminorms of linear operators in Banach spaces |
| Xu-Jia Wang | 261 | Sharp constant in a Sobolev inequality |
| G. Karakostas and Yumei Wu | 269 | Oscillation in dynamical systems |
| E. S. Noussair, C. A. Swanson and Yang Jianfu | 285 | Quasilinear elliptic problems with critical exponents |
| B. Zhang | 303 | Boundedness and stability of solutions of the retarded Liénard equation with negative damping |


## Volume 20 Number 4


| | | |
|---|---|---|
| C. Chicone and F. Dumortier | 315 | Finiteness for critical periods of planar analytic vector fields |
| A. Cellina | 337 | On minima of a functional of the gradient: necessary conditions |
| A. Cellina | 343 | On minima of a functional of the gradient: sufficient conditions |
| T. Domínguez Benavides and R. J. Rodríguez | 349 | Some geometric coefficients in Orlicz sequence spaces |
| K. Kobayashi | 359 | Asymptotic stability in functional differential equations |
| C. T. Kelley and L. Mukundan | 365 | Convergence analysis for the harmonic balance method |

| | | |
|---|---|---|
| JIANG JI-FA and YU SHU-XIANG | 381 | A problem on the stability of a positive global attractor |
| N. G. DE ANDRADE and E. FEIREISL | 389 | Well posedness for the problem of adiabatic shearing of fluids with discontinuous initial data |
| KOK-KEONG TAN and HONG-KUN XU | 395 | Fixed point theorems for Lipschitzian semigroups in Banach spaces |
| SONG FUMIN and SUN JINGXIAN | 405 | Solutions of the second order periodic boundary value problem in a Banach space under the weak* topology |
| H.-M. YIN | 413 | The Lipschitz continuity of the interface in the heat equation with strong absorption |
| Y. S. CHOI and P. J. MCKENNA | 417 | A mountain pass method for the numerical solution of semi-linear elliptic problems |
| H. BELLOUT and F. BLOOM | 439 | Global existence and asymptotic stability of solutions to the Cauchy problem for wave propagation in nonlinear dielectric media |


## Volume 20 Number 5


| | | |
|---|---|---|
| S. MARCHI | 461 | Boundary regularity for weighted quasi-minima—II |
| JONG SOO JUNG and W. TAKAHASHI | 469 | On the asymptotic behavior of infinite products of resolvents in Banach spaces |
| Z. NANIEWICZ | 481 | On the existence of solutions to the continuum model of delamination |
| T. DING and F. ZANOLIN | 509 | Subharmonic solutions of second order nonlinear equations: a time-map approach |
| P. HABETS, M. RAMOS and L. SANCHEZ | 533 | Jumping nonlinearities for Neumann BVPs with positive forcing |
| G. M. LIEBERMAN | 551 | Boundary and initial regularity for solutions of degenerate parabolic equations |
| L. GLANGETAS | 571 | Uniqueness of positive solutions of a nonlinear elliptic equation involving the critical exponent |

## Volume 20 Number 6


| | | |
|---|---|---|
| B. RAO | 605 | Stabilization of Kirchhoff plate equation in star-shaped domain by nonlinear boundary feedback |
| R. T. ROCKAFELLAR | 627 | Dualization of subgradient conditions for optimality |
| T. HARA | 647 | On the Vinograd type theorems for Liénard system |
| I. LASIECKA and R. TRIGGIANI | 659 | Algebraic Riccati equations arising from systems with unbounded input–solution operator: applications to boundary control problems for wave and plate equations |
| D. T. LUC and S. SWAMINATHAN | 697 | A characterization of convex functions |
| V. FERONE and M. R. POSTERARO | 703 | On a class of quasilinear elliptic equations with quadratic growth in the gradient |
| F. CARDIN | 713 | On viscosity and geometrical solutions of Hamilton–Jacobi equations |
| J. M. F. CASTILLO and W. OKRASINSKI | 721 | Boyd index and nonlinear Volterra equations |
| E. FONTICH | 733 | Exponentially small upper bounds for the splitting of separatrices for high frequency periodic perturbations |
| A. B. MACIEL | 745 | On hyperbolic–parabolic equation with a continuous nonlinearity |


## Volume 20 Number 7


| | | |
|---|---|---|
| N. GRENON | 755 | Asymptotic behaviour for some quasilinear parabolic equations |
| D. O'REGAN | 767 | Singular Sturm Liouville problems and existence of solutions to singular nonlinear boundary value problems |
| M. I. KAMENSKIĬ and V. V. OBUKHOVSKIĬ | 781 | Condensing multioperators and periodic solutions of parabolic functional-differential inclusions in Banach spaces |
| J. K. HALE and L. A. C. LADEIRA | 793 | Differentiability with respect to delays for a retarded reaction–diffusion equation |

| | | |
|---|---|---|
| JIA QUAN LIU and ZHI QIANG WANG | 803 | Remarks on subharmonics with minimal periods of Hamiltonian systems |
| N. HAYASHI | 823 | The initial value problem for the derivative nonlinear Schrödinger equation in the energy space |
| I. BEG and N. SHAHZAD | 835 | Random fixed points of random multivalued operators on Polish spaces |
| A. JIMÉNEZ-MELADO and E. LLORÉNS-FUSTER | 849 | A sufficient condition for the fixed point property |
| U. KRAUSE and R. D. NUSSBAUM | 855 | A limit set trichotomy for self-mappings of normal cones in Banach spaces |
| F. S. DE BLASI and G. PIANIGIANI | 871 | Topological properties of nonconvex differential inclusions |


## Volume 20 Number 8


| | | |
|---|---|---|
| M. BOUKROUCHE and G. BAYADA | 895 | Mathematical model. Existence and uniqueness of cavitation problems in porous journal bearing |
| HUAXING XIA and T. SPANILY | 921 | Global existence problem for singular functional differential equations |
| B. WENNBERG | 935 | Stability and exponential convergence in $L^p$ for the spatially homogeneous Boltzmann equation |
| A. HENROT | 965 | Behaviour of the free boundary in electromagnetic shaping when the surface tension vanishes |
| D. O'REGAN | 979 | Nonlinear systems of two point boundary value problems |
| W. VARNHORN | 993 | On Eulerian and Lagrangian representation of steady incompressible fluid flow |
| V. COTI ZELATI and E. SERRA | 1001 | Multiple brake orbits for some classes of singular Hamiltonian systems |
| S. ZAGATTI | 1013 | Metric and topological properties of nondecomposable sets |
| M. FLUCHER | 1021 | Best inequalities for the distance of $L^p$-functions to mean values and weak limits |

J.-B. BAILLON and M. THERA 1029 A new type of convergence with application to Hammerstein's equation

## Volume 20 Number 9

C. LE ROUX and B. D. REDDY 1043 The steady Navier–Stokes equations with mixed boundary conditions: application to free boundary flows

M. SABATINI 1069 An extension to Hadamard global inverse function theorem in the plane

A. GLITZKY 1079 Stability of orbits of solutions of $O(2) \times \mathbb{Z}_2$-equivariant bifurcation problems with variational structure

V. H. MOLL 1095 Threshold phenomenon in a model for platelet aggregation: existence of global solutions and critical multipliers

G. BARLES 1123 Discontinuous viscosity solutions of first-order Hamilton–Jacobi equations: a guided visit

S. HEIKKILÄ and V. LAKSHMIKANTHAM 1135 On the second order mixed quasimonotone periodic boundary value systems in ordered Banach spaces

D.-M. CAO and G. LI 1145 On a variational problem proposed by H. Brézis

J. W. LEE and D. O'REGAN 1157 Existence results for differential delay equations in Banach spaces

## Volume 20 Number 10

K. KOBAYASHI 1183 Stability theorems for functional differential equations

P. WOLFE 1193 Hanging cables with small bending stiffness

T. BARTSCH 1205 Infinitely many solutions of a symmetric Dirichlet problem

J. BANAŚ and K. FRĄCZEK 1217 Conditions involving compactness in geometry of Banach spaces

E. S. P. SIQUEIRA 1231 Asymptotic behavior of the solutions of a nonlinear system of Schrödinger equations

S. JIANG 1245 On global smooth solutions to the one-dimensional equations of nonlinear inhomogeneous thermoelasticity

A. POKROVSKII and D. RACHINSKII 1257 On the existence of a fixed point of the operator acting in the space of continuous functions

A. BAHRI 1261 Another proof of the Yamabe conjecture for locally conformally flat manifolds

## Volume 20 Number 11

R. A. JOHNSON, XINGBIN PAN and YINGFEI YI 1279 Singular ground states of semilinear elliptic equations via invariant manifold theory

U. BESSI 1303 A variational proof of a Sitnikov-like theorem

P. T. CHURCH and J. G. TIMOURIAN 1319 Global cusp maps in differential and integral equations

R. REDHEFFER and W. WALTER 1345 The subgradient in $R^n$

V. WECKESSER 1349 The subdifferential in Banach spaces

E. COMPARINI and A. FASANO 1355 The effect of temperature on the dynamics of a phytoplankton population

W. RZYMOWSKI and A. STACHURA 1369 Curves bounding maximal area

## Volume 20 Number 12

J. M. BORWEIN and M. FABIAN 1373 On generic second-order Gateaux differentiability

R. TORREJÓN 1383 Positive almost periodic solutions of a state-dependent delay nonlinear integral equation

Y. YAN 1417 Attractors and dimensions for discretizations of a weakly damped Schrödinger equation and a Sine–Gorden equation

A. M. FINK, J. A. GATICA and G. E. HERNANDEZ 1453 Eigenvalues of generalized Gelfand models

I Title Page, Volume Contents and Author Index, Volume 20, 1993

# Author Index


Ali Mehmeti, F. 27
Anderssen, R. S. 127

Bahri, A. 1261
Baillon, J.-B. 1029
Banaś, J. 1217
Barles, G. 1123
Bartsch, T. 1205
Bayada, G. 895
Beg, I. 835
Bellout, H. 439
Bessi, U. 1303
Betta, M. F. 63
Bloom, F. 439
Borwein, J. M. 1373
Boukrouche, M. 895
Bugajewski, D. 169

Cao, D.-M. 1145
Cardin, F. 713
Carl, S. 157
Castillo, J. M. F. 721
Cellina, A. 337, 343
Cheng, S. S. 193
Chicone, C. 315
Choi, Y. S. 417
Church, P. T. 1319
Comparini, E. 1355
Coti Zelati, V. 1001

De Andrade, N. G. 389
De Blasi, F. S. 871
Díaz, G. 97
Ding, T. 509
Dominguez Benavides, T. 349
Dumortier, F. 315

Engl, H. W. 127

Fabian, M. 1373
Fasano, A. 1355
Feireisl, E. 389
Ferone, V. 703
Fink, A. M. 1453
Flucher, M. 1021
Fontich, E. 733
Frączek, K. 1217

Gatica, J. A. 1453
Giangetas, L. 571
Glitzky, A. 1079
Goubet, O. 223
Grenon, N. 755

Habets, P. 533
Hale, J. K. 793
Hara, T. 647
Hayashi, N. 823
Heikkilä, S. 157, 1135
Henrot, A. 965
Hernandez, G. E. 1453
Hong-Kun Xu 395
Huaxing Xia 921

Jia Quan Liu 803
Jiang Ji-Fa 381
Jiang, S. 1245
Jiménez-Melado, A. 849
Johnson, R. A. 1279
Jong Soo Jung 469

Kamenskiĭ, M. I. 781
Karakostas, G. 269
Kelley, C. T. 365
Kikuchi, N. 205
Kobayashi, K. 359, 1183
Kok-Keong Tan 395
Krause, U. 855
Kumpulainen, M. 157

Ladeira, L. A. C. 793
Lakshmikantham, V. 1135
Lasiecka, I. 659
Lee, J. W. 1157
Letelier, R. 97
Li, G. 1145
Lieberman, G. M. 551
Lloréns-Fuster, E. 849
Luc, D. T. 697
Lui, R. 11

Maciel, A. B. 745
Macki, J. W. 191
Marchi, S. 461
McKenna, P. J. 417
Mercaldo, A. 63
Moll, V. H. 1095
Mukundan, L. 365

Naniewicz, Z. 481
Nicaise, S. 27
Nistri, P. 191
Noussair, E. S. 285
Ntouyas, S. K. 215
Nussbaum, R. D. 855

Obukhovskiĭ, V. V. 781
Okrasinski, W. 721
O'Regan, D. 79, 767, 979, 1157

Patula, W. T. 193
Pianigiani, G. 871
Pokrovskii, A. 1257
Posteraro, M. R. 703
Precup, R. 1

Rachinskii, D. 1257
Ramos, M. 533
Rao, B. 605
Reddy, B. D. 1043
Reidheffer, R. 1345
Rockafellar, R. T. 627
Rodríguez, R. J. 349
Roux, C. le 1043
Rzymowski, W. 1369

Sabatini, M. 1069
Sanchez, L. 533
Scherzer, O. 127
Serra, E. 1001
Sficas, Y. G. 215
Shahzad, N. 835
Siqueira, E. S. P. 1231
Song Fumin 405
Spanily, T. 921
Stachura, A. 1369
Sun Jingxian 405
Swaminathan, S. 697
Swanson, C. A. 285
Szufla, S. 169

Takahashi, W. 469
Thera, M. 1029
Timourian, J. G. 1319
Tom, M. M. 175
Torrejón, R. 1383
Triggiani, R. 659
Tsamatos, P. Ch. 215

Varnhorn, W. 993

Walter, W. 1345
Weckesser, V. 1349
Wennberg, B. 935
Wolfe, P. 1193

Xingbin Pan 1279
Xu-Jia Wang 261

Yan, Y. 1417
Yang Jianfu 285
Yin, H.-M. 413
Yingfei Yi 1279
Yingfei Yi 1279
Yu Shu-Xiang 381
Yumei Wu 269

Zagatti, S. 1013
Zanolin, F. 509
Zecca, P. 191
Zhang, B. 303
Zhao, W. 249
Zhi Qiang Wang 803


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